

[2] [a] DOMAIN OF $f = \{x \neq \frac{7}{6}\} = (-\infty, \frac{7}{6}) \cup (\frac{7}{6}, \infty)$

$$f'(x) = \underline{-2(6x-7)^3(6)(9x+10)^{\frac{2}{3}} + (6x-7)^2(\frac{2}{3})(9x+10)^{-\frac{1}{3}}(9)} \quad (\frac{1}{2})$$

$$= 6(6x-7)^3(9x+10)^{\frac{1}{3}}[-2(9x+10)+6x-7]$$

$$\textcircled{1} \underline{6(6x-7)^3(9x+10)^{\frac{1}{3}}(-12x-27)} \quad \text{DNE @ } x = -\frac{10}{9} \quad (\frac{1}{2})$$

IN DOMAIN

$$= 0 \text{ IF } \underline{-12x-27=0} \text{ @ } x = -\frac{27}{12} = -\frac{9}{4} \quad \text{IN DOMAIN}$$

CRITICAL NUMBERS $-\frac{10}{9}, -\frac{9}{4}$

SUBTRACT $(\frac{1}{2})$ POINT FOR EACH
ADDITIONAL INCORRECT CRITICAL
NUMBER

[b]

		$-\frac{9}{4}$	$\uparrow$		$-\frac{10}{9}$	$\uparrow$		$\frac{7}{6}$	
			INCLUDES			INCLUDES			
			$x = -2$			$x = -1, 0, 1$			
$6(6x-7)^3$	-		-			-		+	
$(9x+10)^{-\frac{1}{3}}$	-		-			+		+	
$-12x-27$	+		-			-		-	
f'	+	$\longrightarrow$	-	$\longrightarrow$	+			-	

$\textcircled{2}$

$\textcircled{\frac{1}{2}}$ $x = -\frac{9}{4}$ 
LOCAL MAX

$x = -\frac{10}{9}$ 
LOCAL MIN $\textcircled{\frac{1}{2}}$

[3] [a] DOMAIN OF $f = (-\infty, \infty)$

$f'(x)$ EXISTS ON $(-\infty, \infty)$

$$f'(x) = 0 \text{ IF } 20 - 15x = 0 \text{ @ } x = \frac{20}{15} = \frac{4}{3} \quad \left(\frac{1}{2} \right)$$

$$\text{OR } 20 - 3x = 0 \text{ @ } x = \frac{20}{3}$$

CRITICAL NUMBERS $\frac{4}{3}, \frac{20}{3}$

$$[b] \quad f''\left(\frac{4}{3}\right) = 5(48 - 96)(20 - 4)^2 < 0 \rightarrow x = \frac{4}{3} \text{ LOCAL MAX} \quad \left(\frac{1}{2} \right)$$

$\begin{matrix} > 0 & < 0 & > 0 \end{matrix}$

INCORRECT TO SAY
"NOT A MAX OR MIN"

$$\left(\frac{1}{2} \right) \quad f''\left(\frac{20}{3}\right) = 5(240 - 96)(0)^2 = 0 \rightarrow 2^{\text{ND}} \text{ DERIVATIVE TEST DOESN'T APPLY + TELLS US NOTHING} \quad \left(\frac{1}{2} \right)$$

[c] $f''(x)$ EXISTS ON $(-\infty, \infty)$

$$f''(x) = 0 \text{ IF } 36x - 96 = 0 \text{ @ } x = \frac{96}{36} = \frac{8}{3} \quad \left(\frac{1}{2} \right)$$

OR $20 - 3x = 0 \text{ @ } x = \frac{20}{3}$

	$\frac{8}{3}$	$\uparrow$	$\frac{20}{3}$	
		INCLUDES		
		$x = 3, 4, 5, 6$		
$5(36x - 96)$	-	+	+	
$(20 - 3x)^2$	+	+	+	$\left(\frac{1}{2} \right)$
f''	-	$\longrightarrow$ +	+	
	$x = \frac{8}{3}$			
	INFLECTION POINT			$\left(\frac{1}{2} \right)$

[4] f IS CONT ON CLOSED INTERVAL, SO GLOBAL EXTREMA EXIST

$f'(x) = 9x^2 + 12x - 5$ EXISTS ON $[-1, 2]$ SINCE f' POLYNOMIAL

$$= (3x+5)(3x-1) = 0 \text{ @ } x = -\frac{5}{3}, \frac{1}{3}$$

↑
NOT IN $[-1, 2]$

x	$f(x) = 3x^3 + 6x^2 - 5x$
-1	$-3 + 6 + 5 = 8$
$\frac{1}{3}$	$\frac{1}{9} + \frac{2}{3} - \frac{5}{3} = \frac{1}{9} - 1 = -\frac{8}{9}$
2	$24 + 24 - 10 = 38$

GLOBAL MAX @ $x = 2$
GLOBAL MIN @ $x = \frac{1}{3}$

SUBTRACT $\frac{1}{3}$ POINT FOR EACH ADDITIONAL x -VALUE PLUGGED IN

$$\begin{aligned}
 [5][a] \quad \lim_{x \rightarrow -\infty} \frac{4x^3-1}{\sqrt{2x^6-5}} \cdot \frac{\frac{1}{\sqrt{x^6}}}{\frac{1}{\sqrt{x^6}}} &= \boxed{\lim_{x \rightarrow -\infty} \frac{4x^3-1}{\sqrt{2x^6-5}} \cdot \frac{-\frac{1}{x^3}}{\frac{1}{\sqrt{x^6}}}} \quad \left(\frac{1}{2}\right) \\
 &= \boxed{\lim_{x \rightarrow -\infty} \frac{-4 + \frac{1}{x^3}}{\sqrt{2 - \frac{5}{x^6}}}} \quad \left(\frac{1}{2}\right) \\
 &= \frac{-4+0}{\sqrt{2-0}} = \frac{-4}{\sqrt{2}} = \boxed{-2\sqrt{2}} \quad \left(\frac{1}{2}\right)
 \end{aligned}$$

$$\begin{aligned}
 [b] \quad \lim_{x \rightarrow 0^+} (1 - \sin 2x)^{\cot x} &= \lim_{x \rightarrow 0^+} \left[e^{\ln(1 - \sin 2x)} \right]^{\cot x} \\
 &\quad |^{\infty} \text{ INDETERMINATE} \\
 &= \lim_{x \rightarrow 0^+} e^{(\cot x) \ln(1 - \sin 2x)} \\
 &= \boxed{e^{\lim_{x \rightarrow 0^+} (\cot x) \ln(1 - \sin 2x)}} \quad \left(\frac{1}{2}\right) \\
 &= \boxed{e^{-2}} \quad \left(\frac{1}{2}\right)
 \end{aligned}$$

$$\begin{aligned}
 \lim_{x \rightarrow 0^+} (\cot x) \ln(1 - \sin 2x) &= \boxed{\lim_{x \rightarrow 0^+} \frac{\ln(1 - \sin 2x)}{\tan x}} \quad \left(\frac{1}{2}\right) \\
 \infty \cdot 0 \text{ INDETERMINATE} &\quad \quad \quad \frac{0}{0} \text{ INDETERMINATE}
 \end{aligned}$$

$$\begin{aligned}
 &= \boxed{\lim_{x \rightarrow 0^+} \frac{1}{1 - \sin 2x} \cdot (-\cos 2x)(2)} \quad \left(\frac{1}{2}\right) \\
 &\quad \quad \quad \sec^2 x
 \end{aligned}$$

$$= \frac{1(-1)(2)}{1^2} = \boxed{-2} \quad \left(\frac{1}{2}\right)$$

[6] f IS CONT ON $[0, 2]$ AND DIFF ON $(0, 2)$ ① $\frac{1}{2}$
SINCE f IS A RATIONAL FUNCTION WITH DOMAIN $\{x \neq 4\}$

$$f'(x) = -\frac{4}{(x-4)^2} - 1$$

$$\textcircled{\frac{1}{2}} \left[-\frac{4}{(c-4)^2} - 1 \right] = \frac{f(2) - f(0)}{2 - 0} = \frac{-4 - -1}{2 - 0} = -\frac{3}{2} \quad \textcircled{\frac{1}{2}}$$

$$-\frac{4}{(c-4)^2} = -\frac{1}{2}$$

$$8 = (c-4)^2$$

$$\pm 2\sqrt{2} = c - 4$$

$$c = 4 \pm 2\sqrt{2} \quad \textcircled{\frac{1}{2}}$$

$$c = 4 - 2\sqrt{2} \in (0, 2) \quad \textcircled{\frac{1}{2}}$$

$$\approx 4 - 2(1.4) = 1.2$$